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# The Crystal Structures of the Room- and Low-Temperature Modifications of Tris $\left(\eta\right.$-cyclopentadienyl)-di- $\mu_{3}$-thio-tricobalt, $\left[\mathrm{Co}_{3}\left(\eta-\mathrm{C}_{5} \mathrm{H}_{5}\right)_{3} \mathrm{~S}_{2}\right]$ 

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#### Abstract

The crystal structures of the title compound at room temperature and at 130 K are determined. The roomtemperature modification is hexagonal, $P 6_{3} / m$, with $a=$ 9.413 (2), $c=10.094$ (4) $\AA$ and $Z=2$, and is isostructural with $\left[\mathrm{Ni}_{3}\left(\eta-\mathrm{C}_{5} \mathrm{H}_{5}\right)_{3} \mathrm{~S}_{2}\right.$ ] [(Vahrenkamp, Vernon, Uchtman \& Dahl (1968). J. Am. Chem. Soc. 90, 3272-3273], except for the mode of statistical distribution of the $\eta$-cyclopentadienyl rings. The Co-Co distance is $2.691 \AA$ which is definitely longer than those of most of the other trinuclear cobalt complexes, and this difference is explained by the Cotton-Haas theory of metal-metal bonding. The low-temperature modification is also hexagonal with $a=16.080$ (2), $c=29.886$ (2) $\AA$ and $Z=18$; this is a superstructure of the room-temperature modification and the symmetry can be given by the Mischgruppe $P 6_{1} \cup p 3^{\circ}$. The trigonal bipyramid comprising $\mathrm{Co}_{3} \mathrm{~S}_{2}$ is no longer regular and the three $\eta$-cyclopentadienyl rings take three definite orientations.


## Introduction

Tris $\left(\eta\right.$-cyclopentadienyl)-di- $\mu_{3}$-thio-tricobalt, $\quad\left[\mathrm{Co}_{3}(\eta\right.$ $\left.\mathrm{C}_{5} \mathrm{H}_{5}\right)_{3} \mathrm{~S}_{2}$ ], was first prepared by Otsuka, Nakamura \& Yoshida (1968). They also found that this complex is paramagnetic at room temperature and becomes dia-
magnetic below 192.5 K. Sorai, Kosaki, Suga, Seki, Yoshida \& Otsuka (1971) interpreted the mechanism of the phase transition in terms of the cooperative coupling between the orientational motion of the $\eta$ cyclopentadienyl rings (hereafter Cp rings) and the electronic states of the molecule. In this paper, the crystal structures of the title compound at room temperature and at 130 K are reported.

## Determination of the crystal structure of the roomtemperature modification

Crystals of $\operatorname{tris}\left(\eta\right.$-cyclopentadienyl)-di- $\mu_{3}$-thio-tricobalt were kindly provided by Professor Otsuka. They are hexagonal platelets or slender needles, dark brown in color. Weissenberg and oscillation photographs showed the dihexagonal symmetry $6 / \mathrm{mmm}$. The systematic extinctions were observed only for $00 l$ with $l$ odd, corresponding to the space group $P 6_{3} 22$, but it was soon found that the crystal consisted of twins, as will be described later. A crystal approximately $0.2 \times 0.2 \times$ 0.3 mm was used for X -ray data collection on a Rigaku four-circle diffractometer. The crystal data are given in Table 1. The cell parameters were determined with Mo $K \alpha$ radiation ( $\lambda=0.71069 \AA$ ) by a leastsquares fit of 15 reflexions in the range $40^{\circ} \leq 2 \theta \leq$ $50^{\circ}$. The estimated standard deviations of the cell parameters are those from the least-squares calculations. © 1979 International Union of Crystallography

The integrated intensities were obtained for $2 \theta \leq 58^{\circ}$ by the $\omega-2 \theta$ scanning method (scan speed $2^{\circ} \min ^{-1}$ ) using Mo Ka radiation monochromatized with pyrolytic graphite at a take-off angle of $5^{\circ}$. The scan width in $\omega$ was $(1.0+0.4 \tan \theta)^{\circ}$ with background counts of 3 s on either side of the peak. To check instrument and crystal stability, the intensities of three reflexions were measured after every 50 reflexions. Altogether 324 independent reflexions with $\left|F_{o}\right| \geq 3 \sigma(|F|)$ were measured. The usual Lorentz and polarization corrections were applied, but no absorption or extinction corrections were made.

A three-dimensional Patterson function computed from the observed data did not give any clue to a plausible structure. It was found, however, that the diffraction feature of the crystal appeared exactly the same as that reported for the crystal of its Ni congener (Vahrenkamp, Vernon, Uchtman \& Dahl, 1968). It follows that the crystal consists of twins, each of the two component crystals having the symmetry $\mathrm{P6}_{3} / \mathrm{m}$, the $c$ axis in common and (100) as the twinning plane. On the assumption that the crystal structure is isostructural with its Ni congener and that the ratio of the two component crystals is $1: 1$, the structure factor calculations were carried out, ignoring the Cp rings; from these, approximate coordinates of the Co and S atoms were obtained.

The three Co atoms and two S atoms of the molecule form a trigonal bipyramid. A three-dimensional Fourier synthesis phased by these atoms showed the Cp groups as circular haloes with several lumps perpendicular to the lines connecting the center of the molecule and the Co atoms and symmetrically disposed with respect to the plane of the $\mathrm{Co}_{3}$ cluster. Thus, it is concluded that the Cp rings are arranged statistically within their planes so as to give the molecule $\overline{6}$ symmetry. There are a number of possibilities for the statistical arrangement of the Cp rings, but a structure having more than four orientations can be regarded as almost the same as free rotation with respect to the diffraction effect so that this was not considered further. Two types of model, structure ( $a$ ) and structure (b), were considered. Structure ( $a$ ) is a model in which the Cp rings take two orientations statistically in the ring plane

## Table 1. Crystal data of the room-temperature

 modification| Formula | $\left[\mathrm{Co}_{3}\left(\eta-\mathrm{C}_{5} \mathrm{H}_{5}\right)_{3} \mathrm{~S}_{2}\right]$ |
| :--- | :--- |
| $M_{r}$ | $43^{26.22}$ |
| Space group | $P 6_{3} / m$ |
| Unit-cell dimensions $(\AA)$ | $a=9.413(2)$ |
|  | $c=10.094(4)$ |
| $Z$ | 2 |
| $D_{m}\left(\mathrm{Mg} \mathrm{m}^{-3}\right)$ | 1.86 |
| $D_{X}\left(\mathrm{Mg} \mathrm{m}^{-3}\right)$ | 1.870 |
| $\mu$ for $\mathrm{Mo} \mathrm{Ka}^{2}\left(\mathrm{~mm}^{-1}\right)$ | 3.46 |
| Observed reflexions | 648 |
| Independent reflexions | 324 |

with a mutual angle of $180^{\circ}$. Structure (b) is a model in which the Cp rings take three orientations statistically in the ring plane with mutual angles of $120^{\circ}$. A regular pentagon $1.43 \AA$ on an edge was assumed for the Cp ring; $x$ and $y$ for the Co, $z$ for the S atom, $x$ and $y$ for the centroid of the Cp ring, $B$ (isotropic temperature factors) for the C atoms, $B_{i j}$ (anisotropic temperature factors) for the Co and S atoms and $m$ (the fraction of one of the component crystals of the twin) were subjected to least-squares refinement for the two structures. In the least-squares calculations the function $\sum w\left[\left|F_{o}(h k l)\right|^{2}-s^{2}\left|F_{c}(h k l)\right|^{2}\right]^{2}$ was minimized using the methods of Vahrenkamp, Vernon, Uchtman \& Dahl (1968) and Wei, Wilkes \& Dahl (1967), where $s$ is an adjusting factor. The following formulas were used for the diffraction intensity of the twinned composite:

$$
\begin{aligned}
& \left|F_{o}(h k l)\right|^{2}=m\left|F_{o}^{\prime}(h k l)\right|^{2}+(1-m)\left|F_{o}^{\prime}(k h l)\right|^{2},(1 a) \\
& \left|F_{c}(h k l)\right|^{2}=m\left|F_{c}^{\prime}(h k l)\right|^{2}+(1-m)\left|F_{c}^{\prime}(k h l)\right|^{2} .(1 b)
\end{aligned}
$$

The weighting scheme $w=1$ if $0 \leq \sqrt{ }\left|F_{o}\right|^{2} \leq 20 \cdot 0$, otherwise $w=1.0 /\left[1.0+\left(\sqrt{ }\left|F_{o}\right|^{2}-20.0\right) \times 0.836\right]$, was used. The coordinates of the Co and S atoms obtained by these two models both agree to within 0.0002 . With 324 independent intensity data $R_{1}\left(F^{2}\right)$ was 0.104 for structure ( $a$ ) and 0.103 for structure (b), where $R_{1}\left(F^{2}\right)$ is defined as

$$
\begin{equation*}
R_{1}\left(F^{2}\right)=\left.\sum| | F_{o}(h k l)\right|^{2}-\left.s^{2}\left|F_{c}(h k l)\right|^{2}\left|\sum\right| F_{o}(h k l)\right|^{2} . \tag{2}
\end{equation*}
$$

It was impossible to choose between the two structures from the intensity data alone. This is chiefly because of the overlapping of reflexions $h k l$ and $k h l$, which is inherent in the crystal. However, from the structure analysis of the low-temperature modification which will be described in the following section it is concluded that structure (b) is the more plausible structure. The coordinates of the Co and S atoms and of the centroid of the Cp ring are given in Table 2.*

[^0]Table 2. Positional and thermal parameters $\left(\AA^{2}\right)$, with standard deviations in parentheses, for the roomtemperature modification

|  | $x$ | $y$ | $z$ | $B$ | $B_{11}$ | $B_{33}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Co | 0.4973 (2) | 0.1730 (2) | - 3 㐌 ${ }^{\frac{1}{5}}$ |  | 0.0130 (3) | 0.00840 (15) |
| S | + | 1 | 0.3997 (2) |  | $0 \cdot 0130$ (2) | 0.00970 (16) |
| Cp* | 0.305 (2) | -0.018 (2) | $\frac{1}{4}$ | 6.0 (5) |  |  |

*The centroid of the $C p$ ring. Each $C p$ ring takes statistically three orientations given by structure (b).

## Determination of the crystal structure of the lowtemperature modification

For the low-temperature X-ray study, an evaporated-liquid-nitrogen gas gun was used that directed a steady stream of cold gas on to the crystal and its immediate environment. A number of superstructure reflexions were found when the crystal was cooled to the lowtemperature phase. When the crystal was brought back to room temperature all the superstructure reflexions disappeared, so that the transition is confirmed to be reversible. On repeating the cooling and heating, however, it was found that the crystals became ill defined so that it was necessary to replace one crystal by another until sufficient diffraction data to carry out the analysis had been collected. All the data were obtained with Co Ka radiation, maintaining the crystal at $130 \pm 5 \mathrm{~K}$. Fig. 1 shows examples of oscillation photographs taken about the $c$ axis at room temperature and at $130 \pm 5 \mathrm{~K}$. In the low-temperature modification the dimensions of the $a, b$ and $c$ axes are approximately three times as large as those of the room-temperature modification. Weissenberg and oscillation photographs showed $6 / \mathrm{mmm}$ symmetry. As has been mentioned above, the crystal consists of twins and it is most likely that the transition only occurs within the component crystals so that the crystal below the transition temperature also consists of the same type of twin as that of the room-temperature modification. The unit-cell dimensions obtained in the same way as for the room-temperature modification are $a^{\prime}=b^{\prime}=$ 27.852 (2), $c^{\prime}=29.886$ (2) A. [Compare with $3 \times$ $a($ room temperature $)=28.239 \AA, 3 \times c$ (room temperature $)=30.282 \AA$.] The unit cell, therefore, contains $2 \times 3 \times 3 \times 3=54$ molecules.

Since all reflexions $h^{\prime} k^{\prime} l^{\prime}$, for $-h^{\prime}+k^{\prime} \neq 3 n$ are missing, the lattice can be reduced to $a=\left(\frac{2}{3}\right) a^{\prime}+\left(\frac{1}{3}\right) b^{\prime}$, $b=-\left(\frac{1}{3}\right) a^{\prime}+\left(\frac{1}{9}\right) b^{\prime}, c=c^{\prime}$. The lattice constants of the reduced cell are now $a=b=16.080$ (2), $c=$ 29.886 (2) $\AA$ and $Z=18$. The crystal data are shown in Table 3. Fig. 2 shows the sections of the reciprocal lattice constructed from the observed reflexions shown in open circles, where the dotted lines are axes of the reciprocal lattice of the large unit cell. Open circles in Fig. 2 (a) and (b) appear on the same reciprocal-lattice points of the room-temperature modification and they are the fundamental reflexions. Open circles in Fig. 2(c)


Fig. 2. Reciprocal-lattice diagrams for the low-temperature modification.
are the superstructure reflexions, where unusual extinction rules are observed; these can be summarized as follows:

$$
\begin{array}{ll}
h k l:-h+k \neq 3 n & \text { if } l=3 n \\
-h+k=3 n & \text { if } l \neq 3 n  \tag{3}\\
00 l: \quad l \neq 6 n .
\end{array}
$$

The only space group which is compatible with these extinction rules is $P 6_{1}\left(P 6_{5}\right)$, which arises from $l=6 n$ for $00 l$. The extinction rules for the superstructure reflexions suggest that there must be some kind of regularity in the atomic arrangement in addition to the space-group symmetry operations. Suppose we place a scalene, as an exaggerated model for the $\mathrm{Co}_{3}$ cluster, upon a plane. If we produce scalenes by rotations of the scalene around its center, followed by translations,

$$
\begin{equation*}
\operatorname{Rot}(n a) \cdot T\left(n_{1} a^{\prime} / 3+n_{2} b^{\prime} / 3\right), \tag{4}
\end{equation*}
$$

where $a=2 \pi / 3$ and $n=n_{1}+n_{2}$, we obtain an arrangement of the scalenes which has the required translational symmetry parallel to the $X Y$ plane, as shown in Fig. 3. It can be shown that the combined operations, (4), are identical with a set of threefold point operations at those points indicated by small hollow triangles in Fig. 3. The set of these threefold point operations make a plane group, $p 3^{\circ}$.*

It is assumed that each atom of the molecule is related by the symmetry $p 3^{\circ}$ with the corresponding atoms of other molecules in the same plane. If we add a $6_{1}$ axis perpendicular to the molecular layer at the origin indicated in Fig. 3, we obtain an atomic

[^1]Table 3. Crystal data for the low-temperature modification

| Unit-cell dimensions ( $\AA$ ) | $a=b=16 \cdot 080(2)$ |
| :--- | :--- |
|  | $c=29.886(2)$ |
| $Z$ | 18 |
| $D_{x}\left(\mathrm{Mg} \mathrm{m}^{-3}\right)$ | 1.948 |
| Symmetry | $P 6_{1} \cup p 3^{\circ}$ |
| Observed reflexions | 216 |
| Fundamental reflexions | 150 |
| Superstructure reflexions | 66 |
| Temperature of experiment | $130 \pm 5 \mathrm{~K}$ |

arrangement which satisfies all the extinction rules given in (3), as will be explained in the following.

Consider any atom of the molecule in the reduced cell. The atom lies on a plane which has the symmetry $p 3^{\circ}$. This requires that there are two other atoms which are the corresponding atoms of the two other molecules in the asymmetric unit. The coordinates of these atoms can be given by

$$
\begin{equation*}
x, y, z ;-\frac{1}{3}-y, \frac{1}{3}+x-y, z ; \frac{1}{3}-x+y,-\frac{1}{3}-x, z \tag{5}
\end{equation*}
$$

Now, from the $6_{1}$ operations passing through the origin perpendicular to the plane of these three positions, one obtains the following eighteen positions:

$$
\begin{align*}
& x, y, z ;-\frac{1}{3}-y, \frac{1}{3}+x-y, z ; \frac{1}{3}+y-x,-\frac{1}{3}-x, z ; \\
& \bar{y}, x-y, \frac{1}{3}+z ;-\frac{1}{3}-x+y,-\frac{2}{3}-x, \frac{1}{3}+z ; \\
& \frac{1}{3}+x, \frac{2}{3}+y, \frac{1}{3}+z ; y-x, \bar{x}, \frac{2}{3}+z ; \frac{2}{3}+x, \frac{1}{3}+y, \frac{2}{3}+z ; \\
& -\frac{2}{3}-y,-\frac{1}{3}-y+x, \frac{2}{3}+z ; \bar{x}, \bar{y}, \frac{1}{2}+z ; \\
& \frac{1}{3}+y,-\frac{1}{3}-x+y, \frac{1}{2}+z ;-\frac{1}{3}-y+x, \frac{1}{3}+x, \frac{1}{2}+z ; \\
& y, y-x, \frac{5}{6}+z ; \frac{1}{3}+x-y, \frac{2}{3}+x, \frac{5}{6}+z \\
& -\frac{1}{3}-x,-\frac{2}{3}-y, \frac{5}{6}+z ; x-y, x, \frac{1}{6}+z \\
& -\frac{2}{3}-x,-\frac{1}{3}-y, \frac{1}{6}+z ; \frac{2}{3}+y, \frac{1}{3}+y-x, \frac{1}{6}+z \tag{6}
\end{align*}
$$

These positions are shown in Fig. 4. They comprise three sets of the general equivalent positions of $P 6_{1}$. The geometrical structure factors for these eighteen positions clearly show all of the extinction rules of (3), as shown in Table 4.*

The structure is now characterized by the positional and thermal parameters of the 20 non-hydrogen atoms (3Co, 2S, 15C). The intensities of the superstructure reflexions were measured by the visual method using Weissenberg photographs taken with Co $K a$ radiation. Since it was impossible to obtain quantitative intensity data, we had to resort to the trial-and-error method. The three Cp rings of the molecule are no longer equivalent and take three independent orientations. It is most likely that there are three orientations within their planes for these Cp rings in which they are trapped in the low-temperature modification, while in the roomtemperature modification each Cp ring will take any

* See deposition footnote.


Fig. 3. Arrangement of a scalene satisfying the plane-group symmetry $p 3^{\circ}$. Small regular triangles indicate the points of threefold point operations, $p 3^{\circ}$.


Fig. 4. Eighteen general positions generated by the $6_{1}$ axis and $p 3^{\circ}$ as mentioned in the text. Fractions in the figure represent the heights of the general positions along the $c$ axis.
one of these orientations. It is assumed that the three Cp rings are oriented in their planes with the same angle, $120^{\circ}$ (see $\alpha, \beta$, and $\gamma$ in Fig. 7). A fairly good agreement between the observed and calculated intensities of the superstructure reflexions (Fig. 5) was obtained for the parameter values given in Table 5. Here, (1) was used for the expression of intensities of the twin composite. $m$ was assumed to be $\frac{1}{2}$, since it was found to be close to this value in the room-temperature modification. The coordinates of the Co and S atoms are fairly approximate, but not much weight can be placed on those of the C atoms. Mean standard deviations of the coordinates of the Co and S atoms and those of the centroids of the Cp rings are $0.009,0.008$ and 0.006 .

## Results and discussion

## The room-temperature modification

The projection of the structure on to [001] is shown in Fig. 6. It is isostructural with tris $(\eta$-cyclopenta-dienyl)-di- $\mu_{3}$-thio-trinickel (Vahrenkamp, Vernon, Uchtman \& Dahl, 1968), though a reservation is made for the statistical distribution of the Cp rings of the molecule. The $\left[\mathrm{Co}_{3}\left(\eta-\mathrm{C}_{5} \mathrm{H}_{5}\right)_{3} \mathrm{~S}_{2}\right]$ molecule has symmetry $\overline{6}$, and hence the $\mathrm{Co}_{3} \mathrm{~S}_{2}$ cluster forms a regular trigonal bipyramid, and the three Cp rings are bound to


Fig. 5. Observed and calculated intensities for the low-temperature modification.

Table 5. Positional and isotropic thermal parameters for the low-temperature modification

|  | $x$ | $y$ | $z$ | $B\left(\AA^{2}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Co}(1)$ | 0.391 | $0 \cdot 110$ | 0.081 | $2 \cdot 5$ |
| $\mathrm{Co}(2)$ | 0.223 | -0.049 | 0.084 | $2 \cdot 5$ |
| $\mathrm{Co}(3)$ | 0.375 | -0.069 | 0.079 | $2 \cdot 2$ |
| S(1) | 0.333 | 0 | 0.134 | $2 \cdot 5$ |
| S(2) | 0.333 | 0 | 0.032 | $2 \cdot 2$ |
| $\operatorname{Cp}(\alpha)^{*}$ | 0.457 | 0.238 | 0.083 | $6 \cdot 0$ |
| $\operatorname{Cp}(\beta)^{*}$ | 0.096 | -0.120 | 0.083 | $6 \cdot 0$ |
| $\underline{C p}(\gamma){ }^{*}$ | 0.425 | $-0.131$ | 0.083 | 6.0 |

the cluster perpendicularly to the lines connecting the center of the molecule and the Co atoms with their centroids. These Cp rings are statistically distributed within their planes and prefer three orientations with a mutual angle of $120^{\circ}$ (shown as $\alpha, \beta$, and $\gamma$ in Fig. 7), so as to have a horizontal plane of symmetry. Significant interatomic distances and bond angles are shown in Table 6. The Co-Co distance, $2.691 \AA$, found in this complex is longer than that found in $\left[\mathrm{Co}_{3}(\mathrm{CO})_{9} \mathrm{~S}\right], 2.64 \AA$ (Wei \& Dahl, 1967), and is much longer than those reported in many similar trinuclear cobalt complexes, which lie between 2.46 and $2.50 \AA$ $\left\{\mathrm{Co}_{3}(\mathrm{CO})_{10} \mathrm{BH}_{2} \mathrm{~N}\left(\mathrm{C}_{2} \mathrm{H}_{5}\right)_{3}\right.$, Klanberg, Askew \& Guggenberger, 1968; $\left[\mathrm{Co}_{3}(\mathrm{CO})_{9} \mathrm{C}_{2}\right]_{2}$, Dellaca, Penfold, Robinson, Robinson \& Spencer, $1970 ; \mathrm{CH}_{3} \mathrm{CCo}_{3}(\mathrm{CO})_{9}$, Sutton \& Dahl, 1967; $\mathrm{CH}_{3} \mathrm{CCo}_{3}(\mathrm{CO})_{8} \mathrm{P}\left(\mathrm{C}_{5} \mathrm{H}_{5}\right)_{3}$, Brice, Penfold, Robinson \& Taylor, 1970\}. These differences can well be accounted for by the number of electrons occupying the antibonding orbitals of the $\mathrm{Co}_{3}$ cluster, based on Cotton \& Haas's (1964) approximation. The two complexes $\left[\mathrm{CO}_{3}\left(\eta-\mathrm{C}_{5} \mathrm{H}_{5}\right)_{3} \mathrm{~S}_{2}\right]$ and $\left[\mathrm{Co}_{3}(\mathrm{CO})_{9} \mathrm{~S}\right]$ supply 8 and 7 electrons, respectively, and all the other complexes mentioned above only supply 6 electrons to the antibonding orbitals. The $\mathrm{Co}-\mathrm{S}$ distance, $2 \cdot 168 \AA$, can be compared to that reported for $\left[\mathrm{Co}_{3}(\mathrm{CO})_{9} \mathrm{~S}\right]$. The shortest intermolecular atomic distance, $3.59 \AA$, is found between a S atom and a C atom of a neighboring molecule.

## The low-temperature modification

The low-temperature modification is a superstructure of that of the room-temperature modification. The symmetry of the molecule is now 1 , and the $\mathrm{Co}_{3} \mathrm{~S}_{2}$ cluster becomes a scalene bipyramid and the three Cp rings are no longer equivalent but take three definite orientations, with a mutual angle of $120^{\circ}$, shown as $\alpha, \beta$, and $\gamma$ in Fig. 7. There are three molecules in the asymmetric unit. These three molecules are 'equivalent', this being imposed not by the space-group symmetry but by the plane-group symmetry imposed on the three corresponding atoms of the three


Fig. 6. The crystal structure for the room-temperature modification, projected along the $c$ axis.


Fig. 7. Bounded projection of the crystal structure for the lowtemperature modification along the $c$ axis, $z=0-\frac{1}{3}$, based on the coordinates in Table 5.

Table 6. Interatomic distances ( $\AA$ ) and angles $\left({ }^{\circ}\right)$ within the molecule, with standard deviations in parentheses, for the room-temperature modification

| Co-Co | $2.691(4)$ | Co-S-Co | $79.3(4)$ |
| :--- | :--- | :--- | :--- |
| Co-S | $2.168(4)$ | S-Co-Co | $51.4(4)$ |
| S -S | $3.022(4)$ | S-Co-S | $88.8(4)$ |

$\mathrm{Co} \cdots$ centroid of the Cp ring 1.80
molecules. A bounded projection of the structure on to [001] for $z$ from 0 to $\frac{1}{3}$ is shown in Fig. 7, where the $\mathrm{Co}_{3} \mathrm{~S}_{2}$ clusters and the Cp rings drawn in thick lines lie on adjacent layers $c / 6$ above those of the rest. Interatomic distances and angles are given in Table 7. It is

Table 7. Interatomic distances ( $\AA$ ) and angles ( ${ }^{\circ}$ ) within the molecule, with standard deviations in parentheses, for the low-temperature modification

| $\mathrm{Co}(1)-\mathrm{Co}(2)$ | $2 \cdot 63$ (1) | Co-S-Co | 75.2 (9) ~ 81.7 (9) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Co}(2)-\mathrm{Co}(3)$ | $2 \cdot 62$ (1) | Mean | 77.7 |
| $\mathrm{Co}(3)-\mathrm{Co}(1)$ | $2 \cdot 76$ (1) |  |  |
| Mean | $2 \cdot 67$ | $\begin{aligned} & \mathrm{S}-\mathrm{Co}-\mathrm{Co} \\ & \text { Mean } \end{aligned}$ | $\begin{gathered} 47 \cdot 9(9) \sim 56 \cdot 9(9) \\ 51 \cdot 5 \end{gathered}$ |
| $\mathrm{Co}(1)-\mathrm{S}(1)$ | $2 \cdot 20$ (1) |  |  |
| $\mathrm{Co}(2)-\mathrm{S}(1)$ | 2.05 (1) |  |  |
| $\mathrm{Co}(3)-\mathrm{S}(1)$ | $2 \cdot 27$ (1) |  |  |
| $\mathrm{Co}(1)-\mathrm{S}(2)$ | $2 \cdot 12$ (1) |  |  |
| $\mathrm{Co}(2)-\mathrm{S}(2)$ | $2 \cdot 05$ (1) |  |  |
| $\mathrm{Co}(3)-\mathrm{S}(2)$ | $2 \cdot 10$ (1) | , |  |
| Mean | $2 \cdot 13$ |  |  |

interesting to see that though the molecular axis connecting the two S atoms, which was the threefold rotational symmetry axis in the room-temperature modification, has now lost its symmetry properties, each of the two $S$ atoms still has three 'equivalent' C atoms at distances of $\sim 3.6 \AA$ as its immediate neighbors, which are shown by broken lines.

## The symmetry of the low-temperature modification

In the crystal structure of the low-temperature modification, additional local symmetries are found which are exact, as far as the observed extinctions show. These symmetries are closely related to, but do not belong to, the space group of the crystal. The generating symmetry operations of space group $P 6_{1}$, on which the whole atomic arrangement is based, are $t_{10}$, $t_{01}$ and $6_{1}$, where $t_{10}$ and $t_{01}$ are the unit translational symmetries along the $x$ and $y$ axes. Further, the corresponding atoms of the molecules lying on the same layer perpendicular to the $z$ axis form the plane group $p 3^{\circ}$, whose generating symmetry operations are $\mathbf{t}_{10}, \mathbf{t}_{01}$ and $3^{\circ}$. Thus, the set of the whole symmetry operations does not form any group, but can be represented by the Mischgruppe $P 6_{1} \cup p 3^{\circ}$, as is shown schematically in Fig. 8. The existence of crystal structures based on a Mischgruppe has been discussed (Sadanaga, 1963), but the crystal structure of the low-temperature modifi-


Fig. 8. Mischgruppe $P 6_{1} \cup p 3^{\circ}$.
cation presented in this paper is the first example of this kind ever reported.

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[^0]:    * The list of structure factors obtained at room temperature and Table 4 have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34540 (6 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CHI 2 HU , England.

[^1]:    * The notation $p 3^{\circ}$ instead of $p 3$ is used to avoid confusion arising from 3 and $3^{\circ}$. The notation $3^{\circ}$ does not mean the threefold rotational symmetry axis, but it is effective only within a plane.

